

Main theorems in the theory of Markov chains from Hopf algebras (in the sense of [Pan15]). This version: website.

If you spot an error, or know of any other Markov chains built in a similar way, please let me know.

Defining map	any linear map	coproduct-then-product, Hopf powers
Reference	[Pan14]	[DPR14]
construction	Th. 3.1.1	Th. 3.4
diagonalisation	Prop. 3.2.1	Th. 3.15, Th. 3.16, Th. 3.19, Th. 3.20
stationary distribution	Prop. 3.3.1	Prop. 3.21, Prop. 3.23
time-reversal and reversibility	Th. 3.3.2	
strong lumping (projection)	Th. 3.4.1	
weak lumping (projection)	forthcoming	
unidirectionality for free-commutative basis		Sec. 3.3
right eigenfunctions for free-commutative basis		Th. 3.19
probability bounds from above eigenfunctions		
absorption probabilities and terminality of $QSym$		Prop. 3.25, Prop 3.26

References

- [DPR14] P. Diaconis, C. Y. A. Pang, and A. Ram. Hopf algebras and Markov chains: two examples and a theory. *arXiv preprint math/0608208*, 2006.
- [Pan14] C. Y. A. Pang. Hopf algebras and Markov chains. *ArXiv e-prints*, December 2014. A revised thesis.
- [Pan15] C. Y. A. Pang. Card-shuffling via convolutions of projections on combinatorial Hopf algebras. In *27th Annual ACM-SIAM Symposium on Discrete Mathematics*, pages 115–126. Assoc. Discrete Math. Theor. Comput. Sci., Nancy, 2015.

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	descent operators (convolutions-of-projections)
[Pan14]	[Pan15]
Def. 4.3.1, Def. 4.3.4	Def. 3.1
Th. 2.5.1	Th. 4.2 (spectrum only), see separate table
Th. 4.5.1	Th. 4.5
Th. 4.6.1, Th. 4.6.3	
Th. 4.7.1	Th. 4.1
Sec. 5.1.2	
Th. 5.1.9	
Prop. 5.1.11, Prop. 5.1.14	
Sec. 5.1.4	

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